### **DualSPHysics Users Workshop 2016** Welcome



Benedict D. Rogers

School of Mechanical, Aerospace & Civil **Engineering (MACE), University of Manchester** 









Universida<sub>de</sub>Vigo





### Welcome!



We warmly welcome you to the School of Mechanical, Aerospace and Civil Engineering at the University of Manchester

But first **some history**:

Manchester emerged as the world's first industrial city.

Manchester businessmen and industrialists established the **Mechanics' Institute** (Owen's College, UMIST, modern University of Manchester) to ensure their workers could learn the basic principles of science.

University can count **25 Nobel Prize winners** amongst its current and former staff and students

## **Manchester History**

You are in a very historic place for science & engineering!



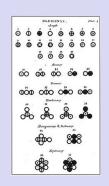


### Role of Manchester in Scientific & Engineering Development

#### **MODERN CHEMISTRY:**

John Dalton (1766 – 1844) foundation of modern atomic theory





### 1st LAW THERMODYNAMICS

mechanical equivalence of heat postulated by **James Prescott Joule** (1819-89)

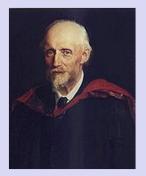


$$dU = \delta Q - \delta W$$

### REYNOLDS NUMBER IN TURBULENT FLOWS:

Osborne Reynolds

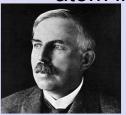
the dimensionless number

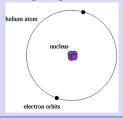


$$Re = \frac{\rho VL}{\mu} = \frac{VL}{v}$$

### **SPLITTING THE ATOM**

Ernest Rutherford at Manchester University discovered how to split the atom in 1919.





### **COMPUTERS**

1st memory programmable computer &

### **Alan Turing**

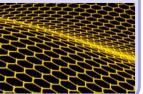




### **GRAPHENE:**

Thinnest supermaterial in the world
Won the Nobel Prize for Physics in 2010







### Role of Manchester in Scientific & **Engineering Development**

Jodrell Bank (Cheshire) a Lovell built world's largest steerable radio telescope just after the Second World War.

Contraceptive pill (1961) and first test tube baby (IVF) was (1978).

World's 1st steampowered mill, opened in 1783 by Richard **Arkwright** for cotton.









The world's first railway station

(Liverpool Road, 1830)



### **VOTES FOR WOMEN:**

Pankhurst founded Women's Social & Political Union in 1903 leading to the Suffragette Movement

World's 1st professional football league set up in 1888 in the **Royal Hotel** Manchester

### **School of MACE**

What happens in MACE?



# School of Mechanical, Aerospace and Civil Engineering (MACE)

- 1000 Undergraduate students on 3 programmes: Mech, Aero & Civil
- 1000 Postgraduate Taught (PGT) Students
- 250 Postgraduate Research (PGR) Students
- 120 Academic Staff + 60 Postdocs

#### Research in MACE:

- Aerospace engineering
- Bio-engineering
- Climate change
- Innovative manufacturing
- Management of projects
- Modelling and simulation
- Nuclear engineering
- Offshore energy and coastal engineering
- Structural and fire engineering



Laser manufacturing

http://www.mace.manchester.ac.uk

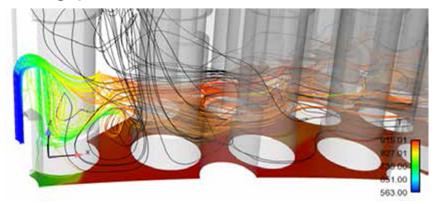
What happens in MACE?



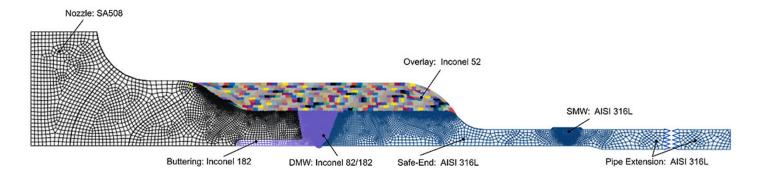
- EDF & University of Manchester established in 2011 a new centre focusing on M&S
- Initially CFD & Computational Solid Mechanics
- Now includes welding technology, long-term structural graphite integrity

### Aims of MaSC:

- Scientific Excellence facilitating world-wide take-up of EDF opensource codes
- Advanced Studies real engineering problems
- Partnership stakeholders
- Skills development training

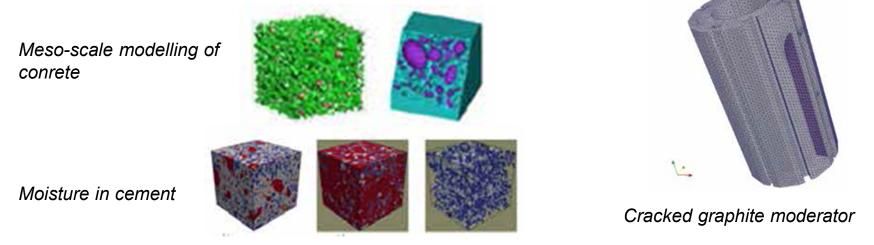


Welding Technology— experimental and numerical investigations of microstructure & weld performance



Mechanics and Physics of Solids – quasi brittle materials, metallic

materials, transport through porous media



And of course SPH!!!



### **Overview**

- Motivation and why SPH
- What is Smoothed Particle Hydrodynamics (SPH)?
- What can SPH do? Why is it revolutionising areas of engineering simulation?
- DualSPHysics
  - Where did it come from?
  - What is a GPU?
  - What can it do?
  - Who are the DualSPHysics team?
  - What SPH activity happens in Manchester

SPHERIC - SPH European Research Interest Community



## **Original Motivation for SPH**

 Free-surface flows are rarely singly connected, e.g. beaches & wave energy devices

### **Breaking waves** on beaches

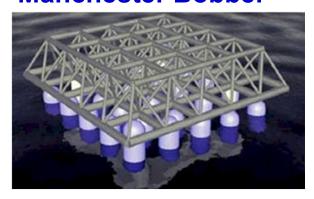


Very complex Multi-phase Multiscale problems

### **Overtopping:**



**Wave Energy Devices: Manchester Bobber** 



**SPH**: Has some distinct advantages in simulating these situations

### **Classical SPH Formulation Example**

**2011 Japanese Tsunami DualSPHysics** 

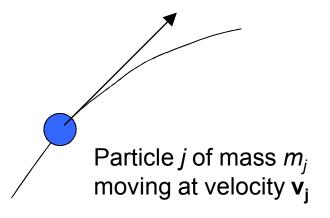
### Meshless methods: Basic Idea of SPH

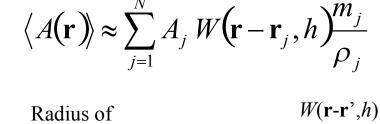
Meshless Our computation points are particles that now move according to governing dynamics, e.g. Navier-Stokes Equations

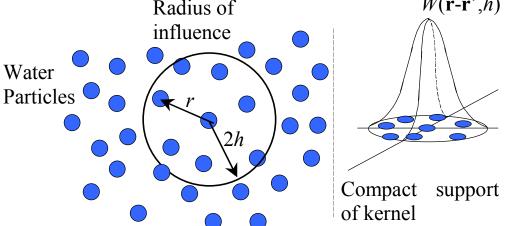
Particles move along a trajectory by integrating in time their velocity & acceleration

Particles possess fluid properties that travel with them, e.g. density, pressure; these can change with time

Local Interpolation (summation) with a weighting function (kernel) around each particle to obtain fluid properties







## Equations of Motion: Approximated by Summation

Navier-Stokes equations:

$$\frac{\mathrm{d}\,\rho}{\mathrm{d}\,t} = -\rho\nabla.\mathbf{v}$$

### Main points are that:

Are recast in

(XSPH - Mo

(i) we do not need to treat the **free surface** 

$$\frac{\mathrm{d}\,\mathbf{r}_i}{\mathrm{d}\,t} = \mathbf{v}_i + \varepsilon \sum_{i}$$

$$\left(\frac{\mathrm{d}\,m_i}{\mathrm{d}\,t}=0\right)$$

(I use i and j to den

(ii) No expensive meshing

(iii) SPH is Meshless & can therefore capture nonlinearity

 $\mathbf{u}_{j} + \mathbf{F}_{i}$ 

This is the classical SPH form, we will change this!

### **SPH for fluid flows**

What can SPH offer?

What can SPH do that other models cannot?



## What can SPH offer the simulation of nonlinear flows?

### SPH is a Lagrangian method

(a) Our computation point are the particles so we can track what happens to the particles which represent the water, the sediment, etc.

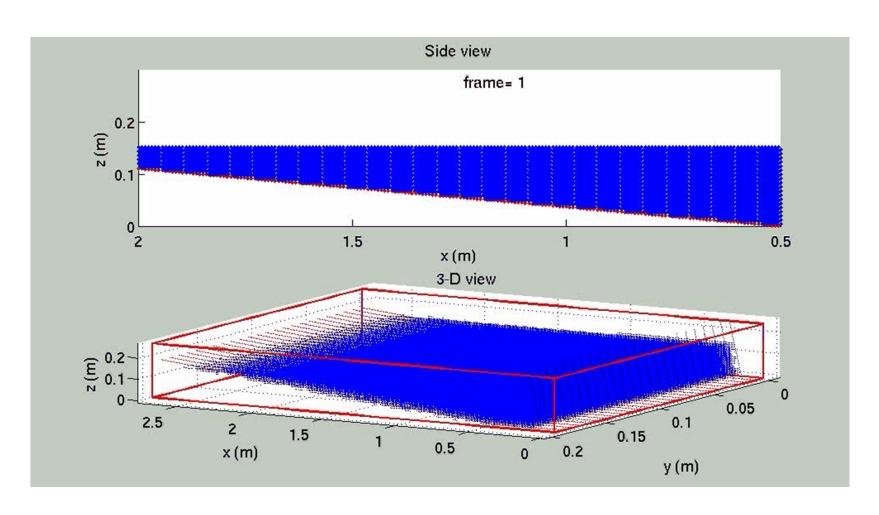
Particle j of mass  $m_j$  moving at velocity  $\mathbf{v_i}$ 

(b) This means we avoid the computation of the nonlinear advection terms within SPH

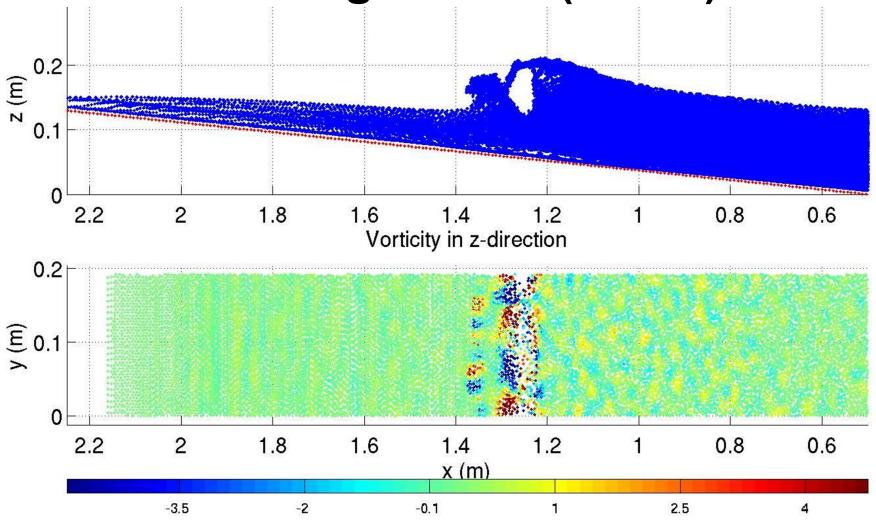
$$\frac{\partial}{\partial t} + u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial z} = \frac{\partial}{\partial t} + \mathbf{u} \cdot \nabla \Rightarrow \frac{D}{Dt}$$

Only the RHS of our equations need SPH treatment

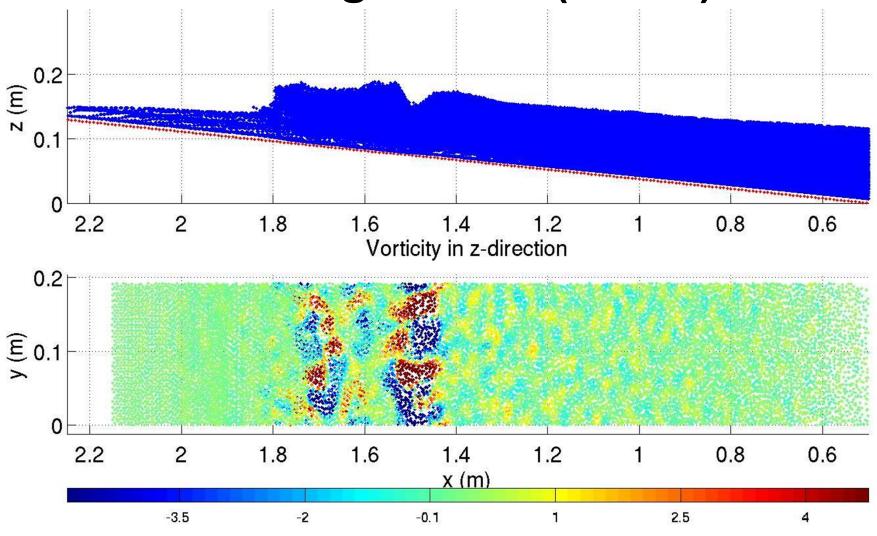
This makes nonlinear phenomena very easy to examine, in particular **FORMATION mechanisms**, eg. mixing ...

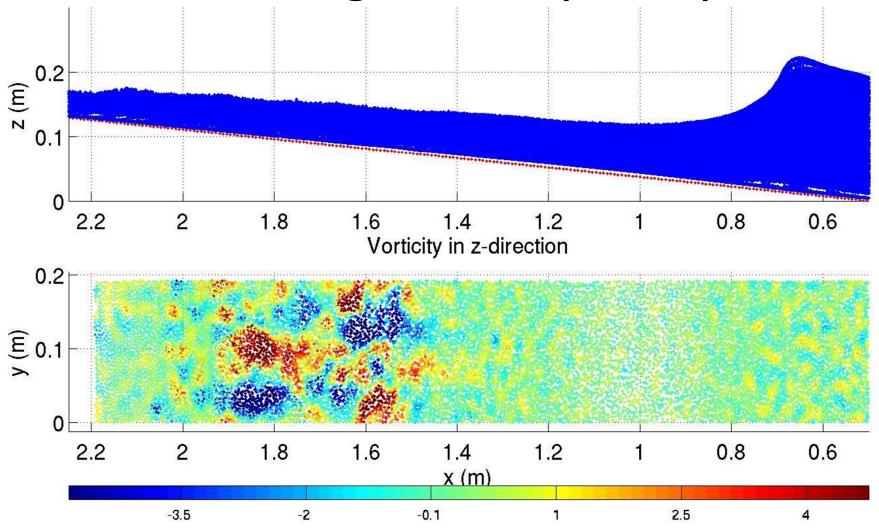


Rogers & Dalrymple (2005)



Initiating turbulence





## **DualSPHysics - what is it?**

Where did DualSPHysics come from?

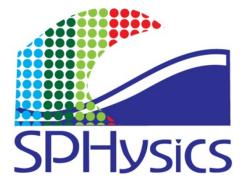
What can DualSPHysics offer?



## **DualSPHysics History - SPHysics**

**FORTRAN** 

CUDA/C++

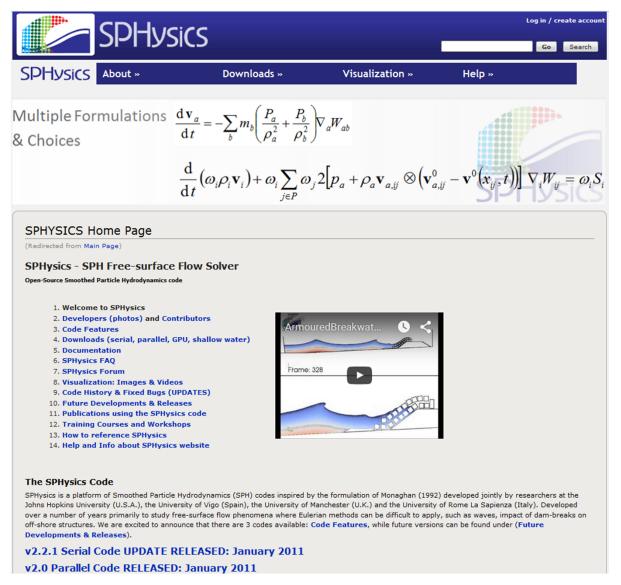








# SPHysics – 1<sup>st</sup> open-source code for free-surface flow (FORTRAN)



Result of 8 years of work

Released in 2007

Collaboration between 4 institutions

- University of Manchester
- Universidade de Vigo
- Johns Hopkins University
- University of Rome La Sapienze

# SPHysics – 1<sup>st</sup> open-source code for free-surface flow (FORTRAN)

- Code had 5 test cases
- 2-D & 3-D
- Choice of options beyond anything else available: kernels, timestepping, formulations & completely open source (mistakes, coding tricks, ...)
- Importantly it was VALIDATED against simple cases

#### **BUT**

- It was very slow
- Restricted to 250,000 particles (simulations took 2-3 weeks)
- Had primitive pre- and post-processing

## **DualSPHysics History - GPUs**



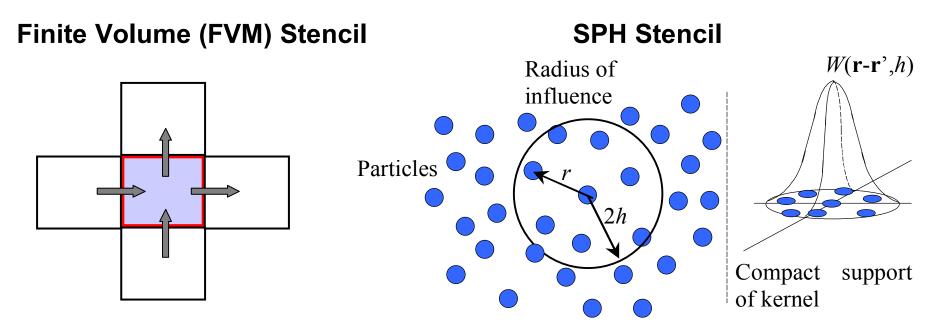


# SPH <u>was</u> prohibitively expensive computationally



## SPH is costly computationally, Why?

- The main problem is due to the interpolation procedure itself
- In Finite Volume, Finite Element & Finite Difference Schemes, the stencil around any cell usually contains only a small number of neighbouring cellsl e.g. In 2-D FVM only 4 neighbouring cells



- In 2-D, each particle typically interacts with 20-50 particles
- In 3-D, each particle typically interacts with 100-400 particles

### Hardware Acceleration: the options

(i) Using parallel (supercomputer) machines with lots of cores (individual CPUs) and divide the work over them

Qu: What's the difference between a parallel machine and a supercomputer?

(ii) FPGAs – Field Programmable Gate Arrays: well used in astrophysics simulations, but expensive and not portable



(iii) **GPUs** – Graphics Processing Units: the **hot topic** of scientific computing



### **TOP SUPERCOMPUTERS IN THE WORLD Nov 2016**

http://www.top500.org

R<sub>max</sub> and R<sub>peak</sub> values are in TFlops. For more details about other fields, check the TOP500 description.

TOP 10 Citac for November 2014

1° Sunway Taihulight (China) 93.0 petaflops/s (consumption: 15371 KW) (CPUs)

3° Titan (USA) 17.5 petaflops/s (consumption: 8209 KW) (with GPUs)

Rank Site System Cores (TFlop/s) (TFlop/s) (kW)

## Energy Efficient GPU co-processors are now a key component in HPC

## Part of computing Emerging Technology 2016 Conference:

http://emit.tech

High Performance Computing Japan M1, Intel Xeon Phi 7250 68C 1.4GHz, Intel Omni-Path

Fujitsu

# There are now several GPU codes ...

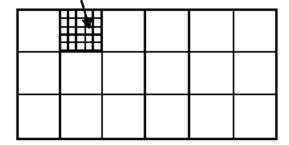


### **Thread**

Identified by threadIdx

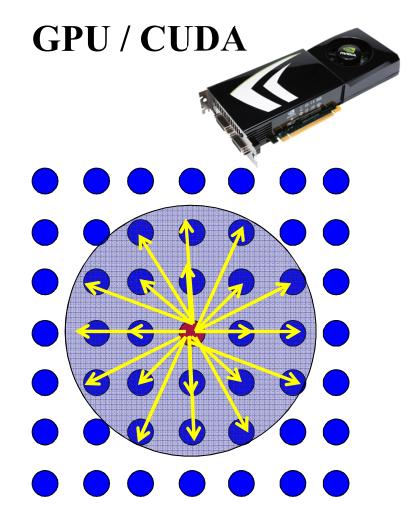
Thread Block ☐ Identified by blockIdx

**Grid of Thread Blocks** 



Result data array

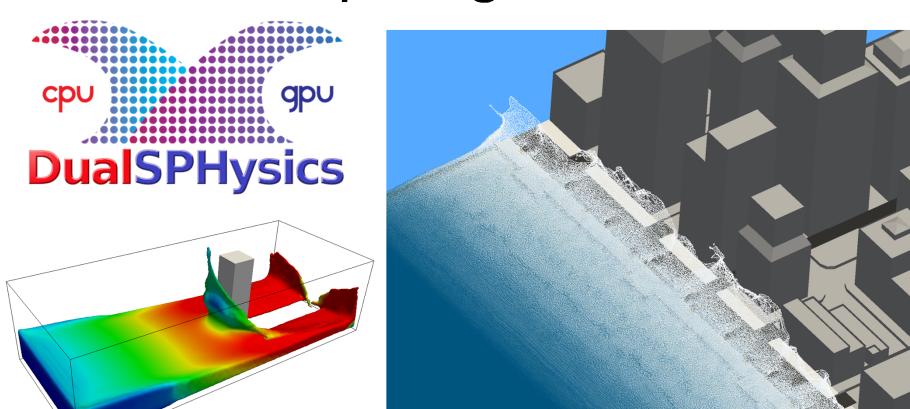
### **SUMMATION SOLUTION**



$$\left(\frac{d\mathbf{u}}{dt}\right)_{i} = \sum_{j} \mathbf{m}_{j} \left(\frac{p_{j}}{\rho_{j}^{2}} + \frac{p_{i}}{\rho_{i}^{2}}\right) \nabla_{i} W_{ij} + \mathbf{g}$$

$$i \rightarrow j$$

# DualSPHysics, new GPU computing on SPH models



A.J.C. Crespo, J.M. Dominguez, A. Barreiro and M. Gómez-Gesteira EPHYSLAB, Universidade de Vigo, SPAIN

B. D. Rogers and D. Valdez-Balderas **MACE**, The University of Manchester, U.K.

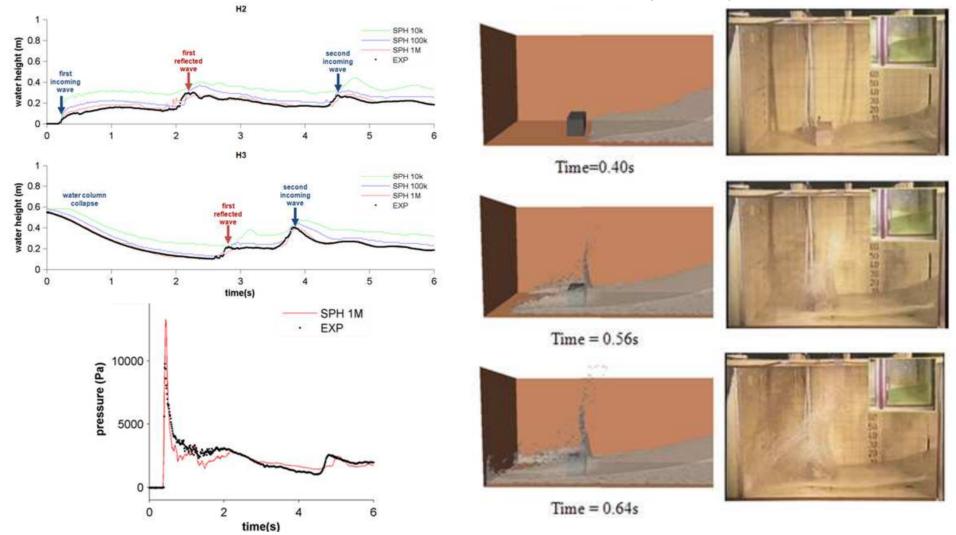
Universida<sub>de</sub>Vigo



### **GPU validation** for a dam break flow impacting on an obstacle

### SPHERIC BENCHMARK TEST CASE 2

Crespo AJC, Dominguez JM, Barreiro A, Gómez-Gesteira M and Rogers BD. 2011. *GPUs, a new tool of acceleration in CFD: Efficiency and reliability on Smoothed Particle Hydrodynamics methods.* PLoS ONE. doi:10.1371/journal.pone.0020685



## The DualSPHysics project team

Who are we?



### **DualSPHysics Project:**

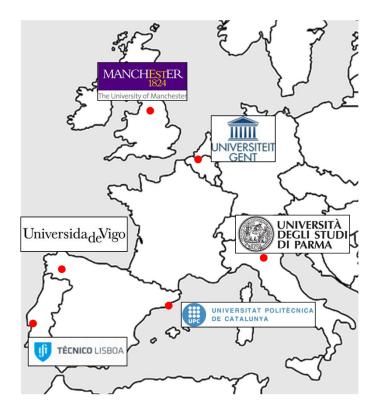
- University of Manchester
- University of Vigo (Spain)
- University of Parma (Italy)
- University of Lisbon (Portugal)
- University of Ghent (Belgium)

### **Websites**

• Free open-source **SPHysics** code:

http://www.sphysics.org

http://www.dual.sphysics.org





Downloaded 15,000+ times: The world's 1<sup>st</sup> open-source plug & play SPH code for free-surface flow

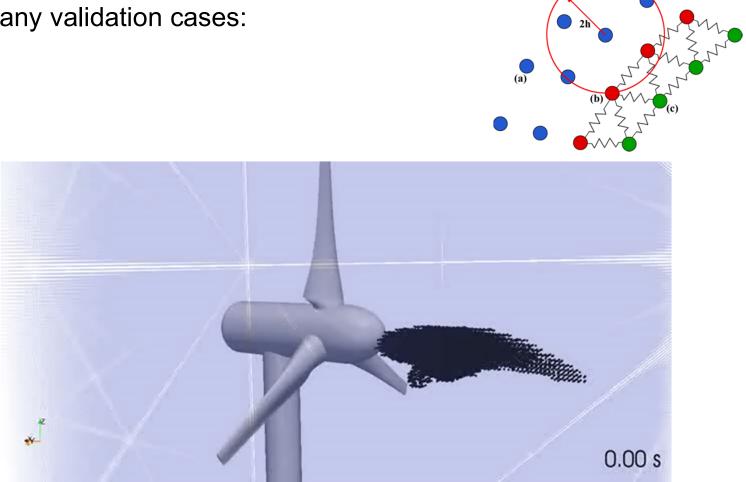
# The DualSPHysics Areas of Activity

What do we do?



## **Combined SPH-MSD Simulation**

After many validation cases:



Involves different Young's moduli of elasticity for different elements of whale

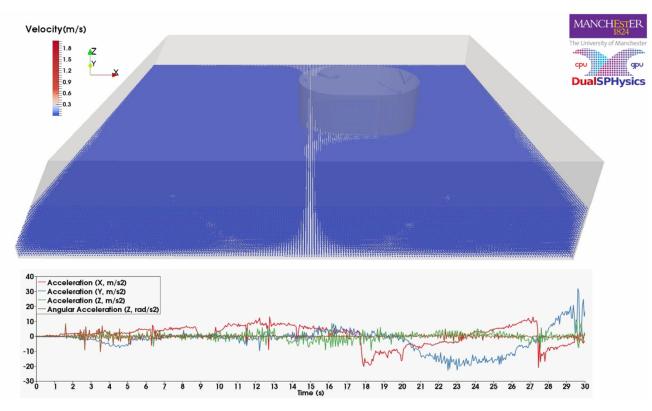
# Fuel-tank sloshing with Leading Motorsport Company (F1)

Real engineering problems are now accessible

Only allowed to show highly simplified geometry

Accelerations are up to 5*g* 

Comparisons with in-tank footage were close.





Longshaw & Rogers (2015), Advances Engineering Software

Funded by Knowledge Transfer Account (KTA), now the IAA

## **Manchester SPH Activity**

What work do we do at Manchester?



## **Better SPH: The options**

Density f

$$\rho_a^{new} = \sum_{b} \rho_b \widetilde{W} \frac{m_b}{\rho_b} \sum_{b} a_b m_{ab} \widetilde{W}_{ab} \frac{m_b}{\rho_b}$$
 Dissipative

2. Volume diffusion methods:

$$\frac{\mathrm{d}\,\rho_i}{\mathrm{d}\,t} = \sum_j m_j \Big(\mathbf{v}_i - \mathbf{v}_j\Big) \nabla_i W_{ij}$$



$$\frac{\mathrm{d} \rho_{i}}{\mathrm{d} t} = \sum_{j} m_{j} \left( \mathbf{u}_{i} - \mathbf{u}_{j} \right) \nabla_{i} W_{ij}$$

$$- \frac{\mathbf{r}_{ij}}{r_{ij}} \cdot \nabla_{i} W_{ij} \left( \frac{c_{ij}}{\rho_{j}} \left( \rho_{j} - \rho_{i} \right) \right)$$

3. Introducing ALE formulations & Riemann solvers

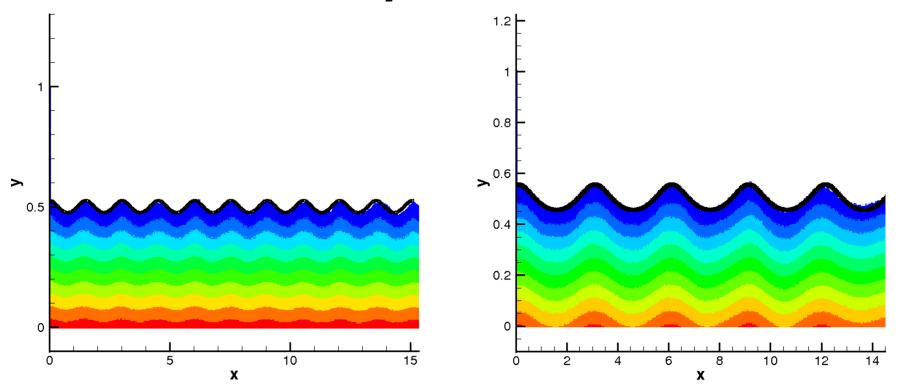
$$\frac{\mathrm{d} \mathbf{v}_i}{\mathrm{d} t} = -\sum_j m_j \left( \frac{P_i}{\rho_i^2} + \frac{P_j}{\rho_j^2} \right) \nabla_i W_{ij} \qquad \qquad \frac{\mathrm{d} \mathbf{v}_i}{\mathrm{d} t} = -\sum_j m_j 2 P_{ij}^* \left( \frac{1}{\rho_i^2} + \frac{1}{\rho_j^2} \right) \nabla_i W_{ij}$$

4. Incompressible SPH (ISPH) + shifting (unique Manchester project)

$$\nabla \cdot \left(\frac{1}{\rho} \nabla p^{n+1}\right)_{i} = \frac{1}{\delta t} \nabla \cdot \mathbf{u}_{i}^{*} \qquad \qquad \delta \mathbf{r}_{s} = -\mathcal{D}\left(\frac{\partial C}{\partial s} \mathbf{s} + \alpha \left(\frac{\partial C}{\partial n} - \beta\right) \mathbf{n}\right)$$

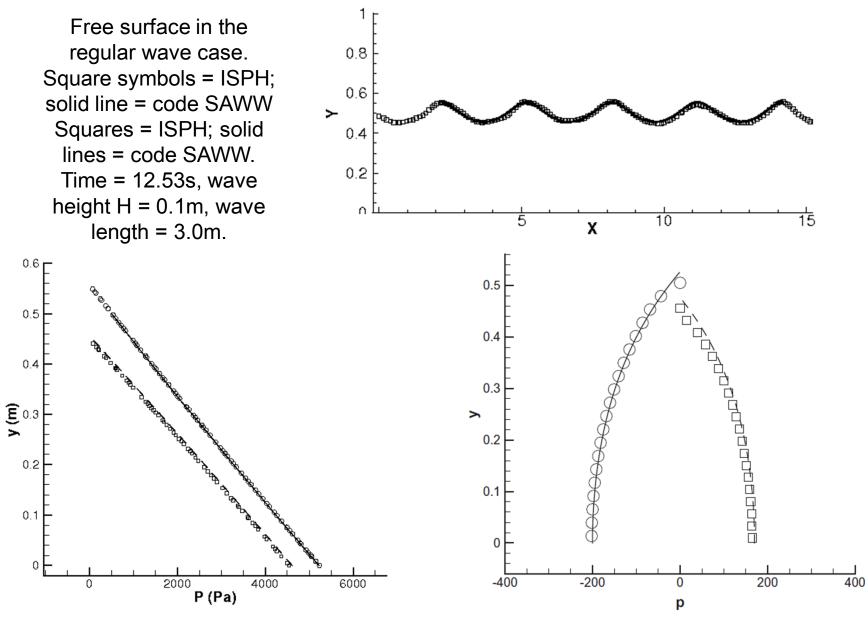
Shift particles to maintain stability.

# Improvement in wave propagation using Incompressible SPH



Comparison of wave propagation along a channel (including pressure contours) with free-surface predictions of SAWW (bold black line).

(a) Wave height H = 0.05m at t = 19.5s. (b) Wave height H = 0.1m at t = 9.75s.



Full & Dynamic Pressure along the vertical line at cross sections, wave crest & trough. Solid lines = wave crest, code SAWW; dashed lines = wave crest, code SAWW; circles = wave crest, ISPH; diamonds = wave crest, ISPH.

## **Eulerian SPH**



## Mixed Eulerian-Lagrangian ISPH

**Increased accuracy and efficiency** 

Fourtakas et al. (2016)

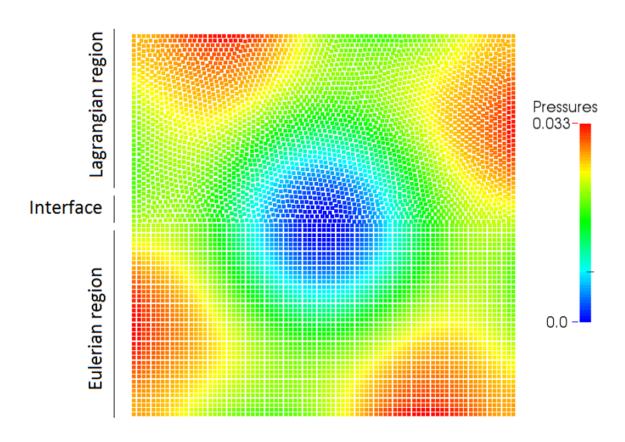
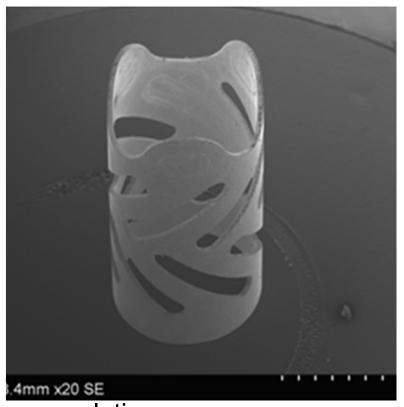


Figure 12. Horizontal and verical velocity profiles of the vortex spin-down case for dx = 0.0125 with Re = 1000 t = 10 s.

Now multi-phase ....



# **Laser Cutting Applications**



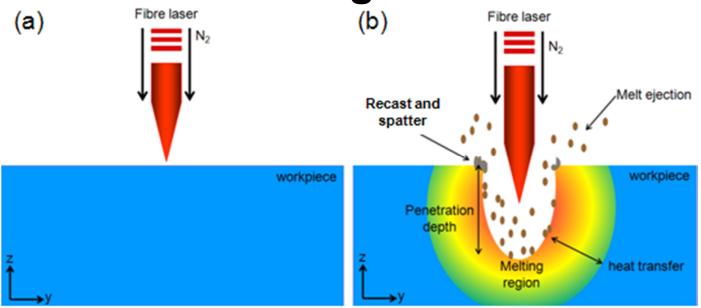
platinum

SEM images of laser cut samples:



- Laser beam heats the surface of the object in very short pulses (typically ms to ps)
- For ms heating, the surface particles increase in Temperature, melt & leave the surface – ideal for SPH
- Backwall damage and debris result
- Assist gas helps the removal of particles within the cut
- Water removes particles under the cut

## **Laser Cutting Process 1**



$$c_{p} \frac{dT}{dt} = \frac{1}{\rho} \nabla (k \nabla T) + Q - Q_{v}$$

$$c_{p,i}\frac{dT_i}{dt} = \sum_{j} \frac{m_j}{\rho_i \rho_j} \left(k_i + k_j\right) \left(\frac{T_i - T_j}{\mathbf{r}_{ij}^2}\right) \mathbf{r}_{ij}. \nabla_i W_{ij} + Q - (Q_v)$$

Laser Beam

$$\rho_m = \rho(T)$$

Laser changes Temperature & density

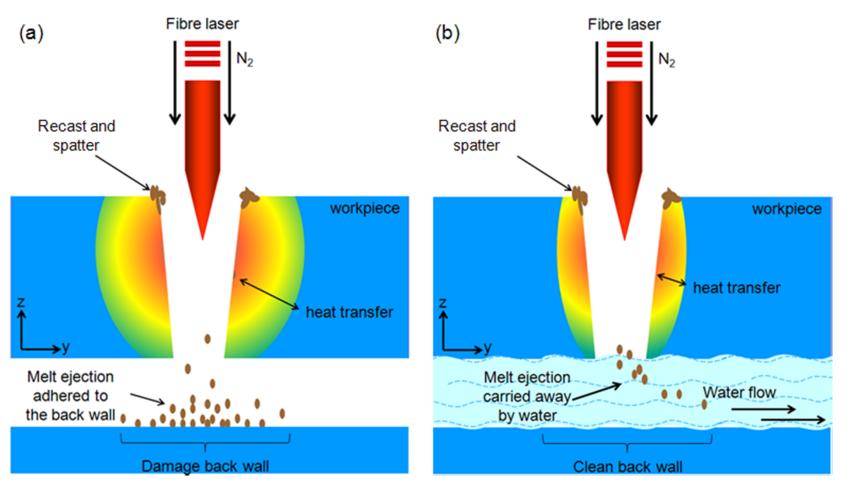
$$P_{vap} = P_0 \exp \left[ \frac{L_v}{R} \left( \frac{1}{T_b} - \frac{1}{T_s} \right) \right] \qquad V_m = \sqrt{\frac{2(P_{vap} + P_{eff})}{\rho_m}}$$

Changes in surface temperature & pressure

$$V_m = \sqrt{\frac{2(P_{vap} + P_{eff})}{\rho_m}}$$

Ejection velocity with assist gas N<sub>2</sub>

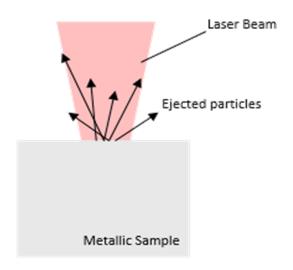
# **Dry & Wet Laser Cutting**



In both cases, the solid phase changes directly into the gaseous phase

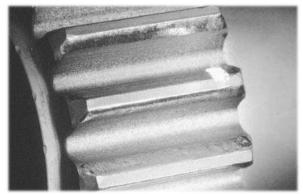
We are not modelling Molecular Dynamics, but use continuum description & SPH to represent the physics.

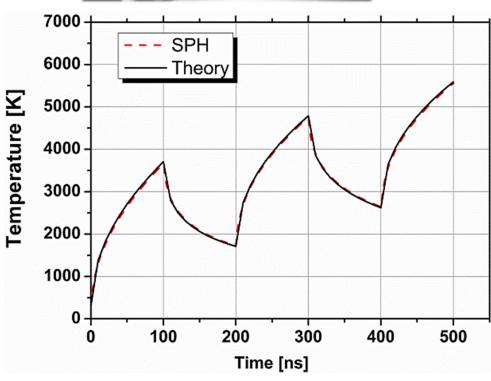
## **Laser Ablation**



ns and ps pulses generated large increases in Temperature

(Al-Shaer et al. 2016 Computational Materials Science)





Psyllaki, P., and Oltra, R., 2000, Materials Science and Engineering: A, 282(1–2), pp. 145-152 ION, J. C. (2005). *Laser processing of engineering materials principles, procedure and industrial application*. Oxford, Boston.

## **SPH free-surface Applications**

**Application: Large-scale Flooding** 

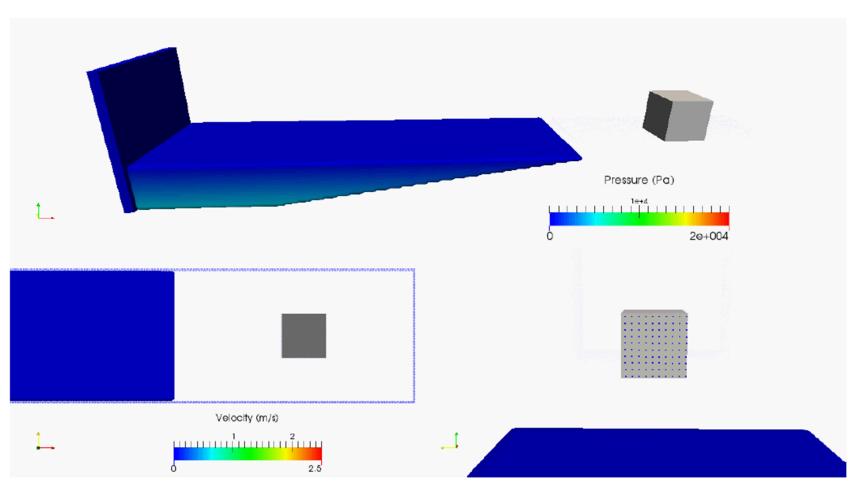
Pringgana et al. 2016, Cunningham et al. 2015 (*Proc. ICE: Engineering and Computational Mechanics*)



# Tsunami-structure interaction modelling with SPH

### **DualSPHysics model simulation:**

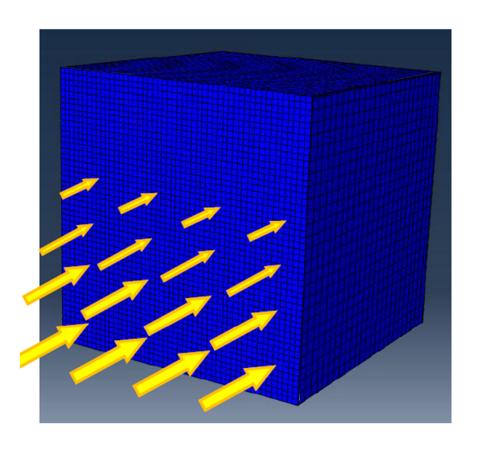
Side view

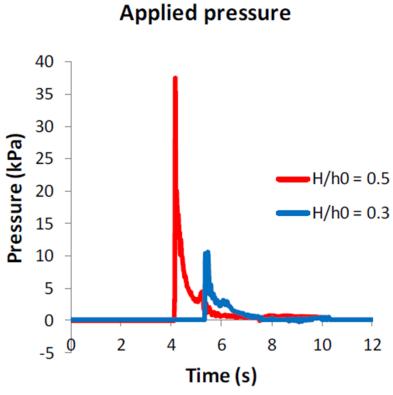


Top view Front view

# Tsunami-structure interaction modelling with SPH

## FE model mesh size and applied loads





Example of load (pressure) time histories at lowest level

# Tsunami-structure interaction modelling with SPH

Stress on structure's components

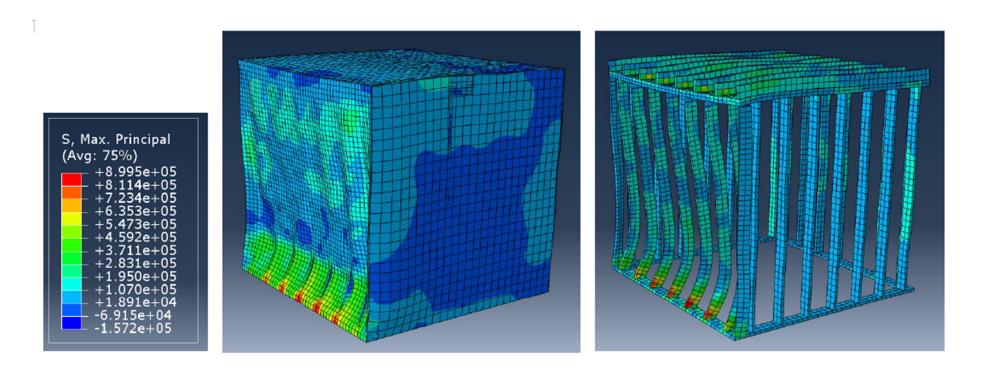
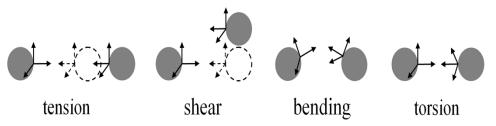


Figure: Stress (Pa) on plywood and studs at the point of maximum impact pressure

Pringgana et al. (2016), Cunningham et al. (2015), Engineering and Computational Mechanics. Awarded Thomas Telford Award by Institution of Civil Engineers

# Vector-based Discrete Element Method (V-Model) for granular structures



Two particle V-DEM model illustrating relative vector orientation under different deformation.

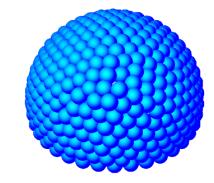
V-Model (Kuzkin & Asonov 2012)

- Vectors on surface of particles define particle orientation relative to connected neighbours.
- Potential energies of bonds are a function of deformations calculated using particle surface vectors.
- Explicit method, time integration similar to SPH.
- Interactions are local making it ideal for computational parallelisation and coupling with SPH.

Original stiffnesses for tension, shear & bending

$$C_a = \frac{EA}{L}, C_S = \frac{GA}{L}, C_b = \frac{EI}{L}$$

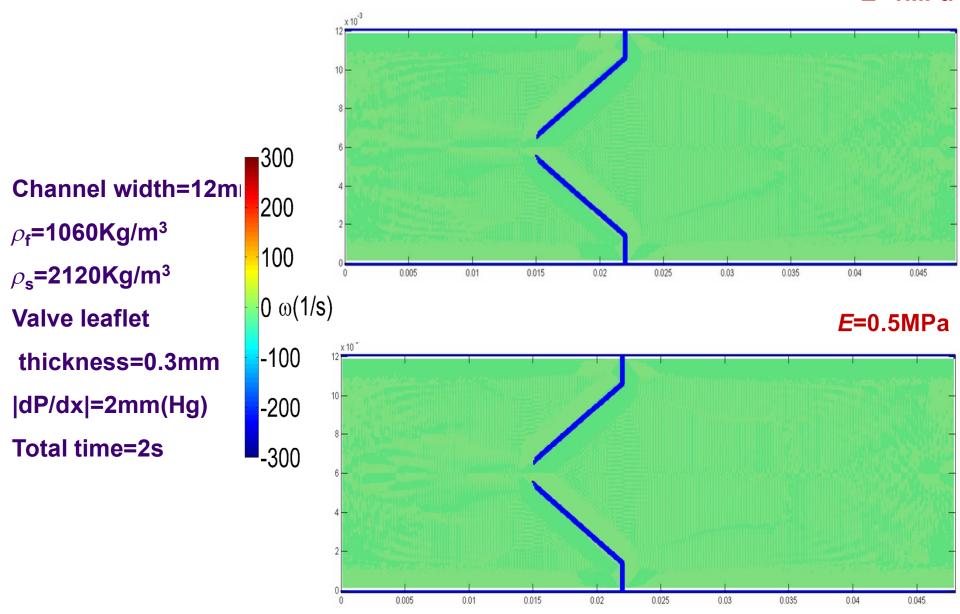
AdioF UNREDISTERED - Www.cif-animator.co



Buckling with point force applied at top of elastic hemi-sphere (Kuzkin 2012)

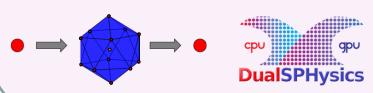
## Idealised flow through deep leg vein

*E*=1MPa



### Manchester SPH: New Developments & Possibilities

**Development of 3-D dynamic particle refinement SPH on GPUs** with U-Vigo & U-Parma using DualSPHysics



Development of SPH for THERMAL HYDRAULIC FLOWS

Development of SPH for Non-Newtonian flows

Development of higherorder convergence SPH Development of SPH for **Bubbly flows**: intumescent paints & steel production

Development of SPH Fluid-Structure Interaction (FSI) Froude Krylov forces; membranes

Development COUPLING SPH with a far-field model with City University (funded by EPSRC)



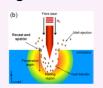
SPH Radius of influence

Water Particles

Meshless & Compact support of kernel

nonlinear simulation technique  $A(\mathbf{r}) \approx \sum_{j=1}^{N} A_j W(\mathbf{r} - \mathbf{r}_j, h) \frac{m_j}{\rho_j}$ 

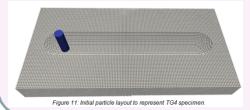
**Development of** 3-phase laser cleaning & keyhole processing SPH model

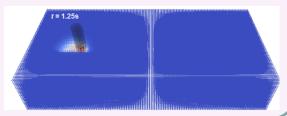


Application to Soil Erosion with University of Brasil for agriculture (funded by EPSRC)

Development for granular flows and Hot Isostatic Pressing (HIP) (funded by EPSRC NNUMAN)

#### Development of multi-phase SPH for WELDING on GPUs





## Manchester MaSC SPH Group 2016

#### **Lead Academic Staff**

Dr Benedict Rogers
Prof. Peter Stansby
Dr Steve Lind

#### **Research Assistants**

Dr Athanasios Mokos Dr Georgios Fourtakas Dr Xiaohu Guo (STFC)

#### **Permanent Visitors**

Dr Alex Crespo Dr Jose Dominguez Dr Renato Vacondio

#### **Collaborating Academic Staff**

Prof. Dominique Laurence
Prof. Yong Wang
Dr Lee Cunningham
Dr Alistair Revell

#### **Research Students**

Ahmad Wael al-Shaer Alex Chow Sam Hunter Annelie Baines

Aaron English

Katy Walton

+ 11 PhDs graduated







## **SPHERIC**

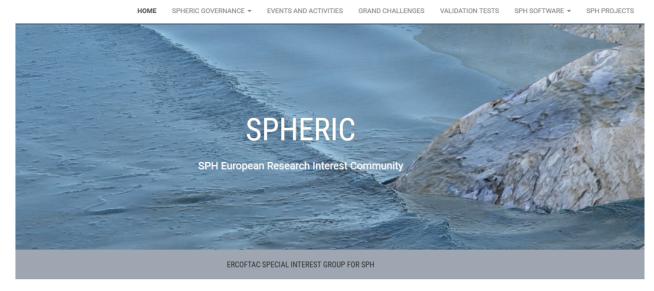
International Research Initiative: <a href="https://spheric-sph.org">https://spheric-sph.org</a>

- Founding members
- Steering Committee
- Webmasters

BDR: 2005-2015

AJC: 2015 -

- -Chair (2015 2020)
  - -11 International Workshops
  - -2017 in Ourense
  - -Training Day



#### Welcome to SPHERIC

SPHERIC is the international organisation representing the community of researchers and industrial users of Smoothed Particle Hydrodynamics (SPH).

As a purely Lagrangian technique, SPH enables the simulation of highly distorting fluids and solids. Fields including free-surface flows, solid mechanics, multi-phase, fluid-structure interaction and astrophysics where Eulerian methods can be difficult to apply represent ideal applications of this meshless method.

Regular Newsletters



- 75 Institutions are members: universities, government research labs & industrial companies

# Key Issues in SPH: SPHERIC Grand Challenges & then some

- Convergence and Accuracy this is still in development and not proven theoretically (the fully Lagrangian approach currently has a 2<sup>nd</sup>order upper bound)
- 2. Numerical stability this is still unproven
- 3. Boundary Conditions probably the worst culprit of all problems for free-surface flow
- 4. Adaptivity efficient simulations are key for engineering application

- Very small timestep & Formulation for simulation involving many freesurface wave problems – SPH is good & bad: OTHER METHODS?
- Turbulence a very difficult topic in its own right is yet to receive comprehensive investigation

### **SPH Vision for Free-surface flow:**

# Research Activity

SPHERIC Grand Challenges

Convergence

**Stability** 

Robust boundary conditions: solid, open, free surface

Particle Adaptivity: dynamic & automatic with uniform error distribution

**New formulations** 

Collaboration & Dialogue in SPH Community

Fast SPH simulations on energy efficient computing

Standards for SPH

Rigorous validations with high quality & repeatable reference data/solutions

> Education & Training

Open-source codes & future proofing

Identification of cases where SPH excels/fails

**Turbulence** 

Multi-phase and Multifluid formulations

Coupling

Fluid-structure interaction

Industrial Activity

Challenging Applications

Industrial requirements

Integrate SPH into design methodologies

Funding University Research

**Good practice** 

Robust & Stable SPH used in Industry & Research

Violeau & Rogers (2016), "SPH for free-surface flow: past, present and future", Journal of Hydraulic Research.

## **DualSPHysics Users Workshop**

**Workshop origins** 

Workshop structure



## **DualSPHysics Users Workshop**

#### **Origins:**

- Since release, DualSPHysics has been downloaded 1000s times
- DualSPHysics website has a users' forum where a lot of questions get asked about how to use the code.
- We often get approached by both industrial companies & academic organisations who ask us <u>one question repeatedly</u>:

### "Can SPH do this?"

### **Aims of Workshop:**

- Hear how other users of DualSPHysics are using the code
- Hear the latest developments from the DualSPHysics team
- Give you an opportunity to make suggestions to help guide the future development of the DualSPHysics project.

## **DualSPHysics v4 New Features**

- Structure of the CPU and GPU code:
- Optimisation of the size of blocks for execution of CUDA kernels:
- Double precision
- Improved formulation for adding external forces
- Movement from external file for rotation
- Coupled SPH & DEM
- Multi-Phase soil-water
- Novel Shifting algorithm
- Automatic wave generation
- More powerful GenCase using OpenMP
- New options in MeasureTool for moving probe points
- Force computation
- More information for floating bodies and motion analysis
- Store information with variable output time
- New properties for different type of fluids or boundaries
- New variables in post-processing tools defined by the user
- Alternative building method via CMAKE (<a href="https://cmake.org/">https://cmake.org/</a>)

# Thank you

### Acknowledgments

- U-Man: Abouzied Nasar, Alex Chow, George Fourtakas, Athanasios Mokos, Gede Pringgana
- U-Vigo: Alex Crespo, Jose Dominguez, Moncho Gomez-Gesteira, Anxo Barreiro
- Flanders Hydraulics: Corrado Altomare
- U-Parma: Renato Vacondio
- U-Lisbon: Ricardo Canelas

### **Websites**

- Free open-source DualSPHysics code: http://www.dual.sphysics.org
- SPHERIC = SPH European Research Interest Community: http://wiki.manchester.ac.uk/spheric



